

**Intermediate Algebra Skill**  
**Solving 3 x 3 Linear System by Gaussian Elimination**

Solve the following Linear Systems of Equations by Gaussian Elimination:

$$1) \begin{cases} 4x + 2y - 6z = 34 \\ 2x + y + 3z = 3 \\ 6x + 3y - 3z = 37 \end{cases}$$

$$8) \begin{cases} 2x - 4y + z = 10 \\ x + 2y - z = 1 \\ -x - 3y + 2z = 0 \end{cases}$$

$$2) \begin{cases} 3x - y + z = -1 \\ 2x + 3y + z = 4 \\ 5x + 4y + 2z = 5 \end{cases}$$

$$9) \begin{cases} 3x + y - z = 4 \\ x + 2y + 2z = 5 \\ 4x + y - z = 3 \end{cases}$$

$$3) \begin{cases} 2x + y + z = -2 \\ 2x - y + 3z = 6 \\ 3x - 5y + 4z = 7 \end{cases}$$

$$10) \begin{cases} 5x + 6y - 5z = -1 \\ 3x - 4y - 3z = 7 \\ -2x + 5y + z = -4 \end{cases}$$

$$4) \begin{cases} 6x + 2y - 4z = 15 \\ -3x - 4y + 2z = -6 \\ 4x - 6y + 3z = 8 \end{cases}$$

$$11) \begin{cases} 2x + 3z = 1 \\ 3x - 5y = 10 \\ 4y - 3z = 13 \end{cases}$$

$$5) \begin{cases} 3x + 3z = 0 \\ 2x + 2y = 2 \\ 3y + 3z = 3 \end{cases}$$

$$12) \begin{cases} 3y + 4z = 6 \\ 3x - 5z = 3 \\ 2x + 5y = 2 \end{cases}$$

$$6) \begin{cases} x + 3y - 3z = 12 \\ 3x - y + 4z = 0 \\ -x + 2y - z = 1 \end{cases}$$

$$13) \begin{cases} \frac{1}{2}x + \frac{1}{3}y = 4 \\ \frac{1}{2}y - \frac{1}{4}z = 1 \\ \frac{1}{4}x + \frac{1}{2}z = 5 \end{cases}$$

$$7) \begin{cases} x + y + z = 3 \\ 2x - y - z = 0 \\ x + 2y - z = -1 \end{cases}$$

$$14) \begin{cases} \frac{1}{3}x - \frac{1}{3}z = -2 \\ \frac{1}{6}y + \frac{1}{3}z = 7 \\ \frac{2}{3}x + \frac{1}{4}y = 9 \end{cases}$$

***Intermediate Algebra Skill***

**Answers to Solving 3 x 3 Linear System by Gaussian Elimination**

1) (*Dependent*)

2)  $(-1, 1, 3)$

3)  $(-3, 0, 4)$

4)  $\left(2, -\frac{1}{2}, -1\right)$

5)  $(0, 1, 0)$

6)  $(3, 1, -2)$

7)  $(1, 0, 2)$

8)  $(3, -1, 0)$

9)  $(-1, 5, -2)$

10)  $(-2, -1, -3)$

11)  $(5, 1, -3)$

12)  $(6, -2, 3)$

13)  $(4, 6, 8)$

14)  $(9, 12, 15)$